

# Equations and PFTs for soil thermal properties in LSMs: Implications for the energy balance

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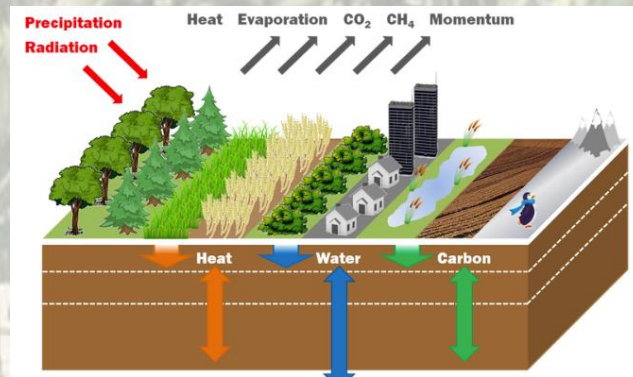
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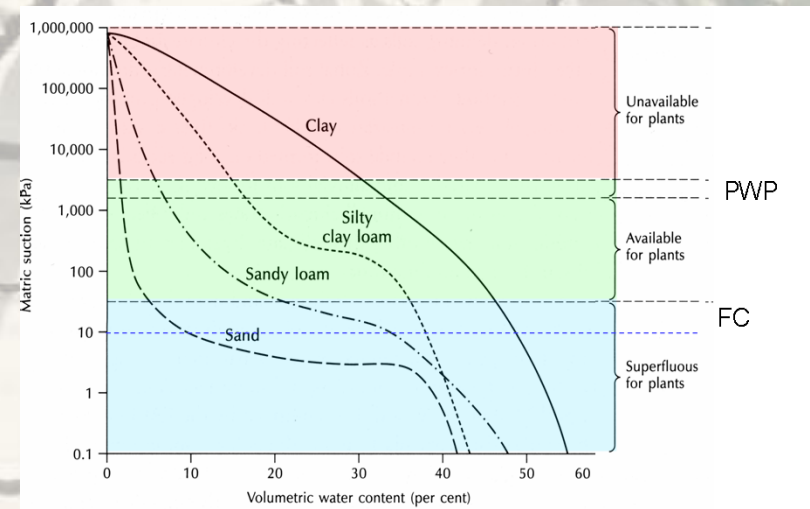
**SURFEX-ISBA:** Aaron Boone and Sebastien Garrigues

## OVERVIEW

- Joint ISMC and GEWEX communities: Initiatives to improve soil and subsurface processes in current climate and hydrological models
- Evaluation of pedotransfer functions and related functional descriptions for calculation of hydraulic and thermal soil properties in global climate models.



land surface model



## THERMAL CONDUCTIVITY, $\lambda$

- Soil thermal conductivity depends on dry,  $\lambda_{dry}$ , and saturated conductivity,  $\lambda_{sat}$ , in combination with a soil moisture dependent weighting function,  $F_\theta$
- Equations are required to estimate  $\lambda_{dry}$ ,  $\lambda_{sat}$  and  $F_\theta$
- These parameters, and their intrinsic parameters all require 'thermal' PFTs

Most LSM models use:

$$\lambda = F_\theta \lambda_{sat} + (1 - F_\theta) \lambda_{dry}$$

Weighting function

One uses:

$$\lambda = \lambda_0 + \lambda_1 F_\theta + \lambda_2 [F_\theta]^2$$



WEIGHTING FUNCTION,  $F_\theta$ 

- The weighting function,  $F_\theta$ , is often the Kersten number,  $K_e$ , which is dependent on the relative saturation,  $S_e$
- Constant  $\gamma$  varies between models
- $S_e$  depends on moisture content,  $\theta$ , and saturated moisture content,  $\theta_{sat}$ , and residual SMC,  $\theta_r$  (for VG).

Most LSMs:  $F_\theta = \text{Kersten number}, K_e$

$$K_e = \gamma \log(S_e) + 1$$

$$F_\theta = S_e \text{ for 2 others}$$

where  $\gamma$  is generally one, but for some models is set to 0.7 for coarse soils.

Others use  $\gamma = 0.7$  for  $0.05 < S_e \leq 0.1$ .

Clapp & Hornberger/Brooks & Corey

$$S_e = \frac{\theta}{\theta_{sat}}$$

Van Genuchten, VG

$$S_e = \frac{\theta - \theta_r}{\theta_{sat} - \theta_r}$$

## DRY THERMAL CONDUCTIVITY, $\lambda_{dry}$

- generally dependent on (some of) the soil texture fractions (sand, silt, clay), either explicitly or implicitly (via soil class look-up tables, LUTs).
- Porosity,  $\theta_{sat}$ , is an important parameter, and depends on hydraulic PFTs (in blue)

Alternatively

$$\lambda_{dry,min} = 0.19$$

Most LSMs use Johansen (1975), as also used by Peters-Lidard et al. (1998)

$$\lambda_{dry,min} = \frac{0.135\rho_{min} + 64.7}{\rho_{min} - 0.947\rho_{b,min}^d}$$

One uses (Cox et al., 1999)

$$\lambda_{dry,min} = \lambda_{air}^{\theta_{sat}} X_{cl} X_{sa} X_{si}$$

$$X_j = C_j f_j^{(1-\theta_{sat})}$$

$C_j$  is a constant (1.16 for clay, 1.57 for silt and sand), and  $f_j$  is **the fraction of  $j$  = clay, silt, or sand**

Or Lu et al., 2007

$$\lambda_{dry,min} = -0.56\theta_{sat} + 0.51$$

## SATURATED THERMAL CONDUCTIVITY, $\lambda_{sat}$

- The saturated thermal conductivity generally depends on the thermal conductivities of the solid soil material,  $\lambda_{soil}$ , liquid soil water,  $\lambda_{liq}$ , and ice,  $\lambda_{ice}$ , sometimes on  $\lambda_{air}$ .

Most LSMs use (from Johansen, 1975?):

$$\lambda_{sat} = \lambda_{soil}^{1-\theta_{sat}} \lambda_{ice}^{\theta_{sat}-\theta_u} \lambda_{liq}^{\theta_{sat}^u}$$

Soil solid conductivity (see next slide)

One uses

$$\lambda_{sat} = \lambda_{dry} \left( \lambda_{liq}^{\theta_{sat}^u} \lambda_{ice}^{\theta_{sat}^f} \right) / \lambda_{air}^{\theta_{sat}}$$

Or

$$\lambda_{sat} = \begin{cases} 1.58 & \lambda_{dry} < 0.25 \\ 1.58 + 12.4(\lambda_{dry} - 0.25) & 0.25 < \lambda_{dry} < 0.3 \\ 2.2 & \lambda_{dry} > 0.3 \end{cases}$$



## SOIL SOLID THERMAL CONDUCTIVITY, $\lambda_{soil}$

- The saturated thermal conductivity generally depends on the thermal conductivities of the solid soil material,  $\lambda_{soil}$ , liquid soil water,  $\lambda_{liq}$ , and ice,  $\lambda_{ice}$ , sometimes of  $\lambda_{air}$ .

$$f_{qu} = 0.038 + 0.0095f_{SA}$$

$\lambda_{qu}$  the thermal conductivity of quartz, having a value of 8.8 or 7 W m<sup>-1</sup> K<sup>-1</sup>  
 $\lambda_o$  is the thermal conductivity of other minerals, generally set to 2 or 3 W m<sup>-1</sup> K<sup>-1</sup>

In a number of LSMs,  $\lambda_{soil}$  is assumed to be dependent only on the thermal conductivity of the mineral soil solids as given by (Johansen, 1975):

$$\lambda_{soil} = \lambda_{qu}^{f_{qu}} \lambda_o^{1-f_{qu}}$$

Some use:

$$\lambda_{soil} = \frac{\lambda_{qu}f_{sand} + \lambda_{clay}f_{clay}}{f_{sand} + f_{clay}}$$

$$\lambda_{soil} = 7.0$$

$$\lambda_{soil} = 3.44$$

## SOIL HEAT CAPACITY, $C_h$

- Theory (e.g. Van Wijk & de Vries, 1963) states soil heat capacity depends on the specific heat capacities ( $c_i$ ) of the solid soil material, liquid soil, water, ice, and air, their densities ( $\rho_i$ ) and volume fractions ( $\phi_i$ ).
- Alternatively we can use the volumetric heat capacity
- Some models use a constant  $C_h$  ( $= 2.19 \times 10^6$ ; independent of soil type), i.e. its values remain unchanged despite changes in  $\theta$ , whereas others uses values ranging between  $1.93 \times 10^6$  for sand to  $2.48 \times 10^6$ , for clay.

$$C_h = \underbrace{\phi_{min} \rho_{min} c_{min}} + \underbrace{\phi_{org} \rho_{org} c_{org}} + \underbrace{\phi_{liq} \rho_{liq} c_{liq}} + \underbrace{\phi_{ice} \rho_{ice} c_{ice}} + \underbrace{\phi_{air} \rho_{air} c_{air}}$$

$$C_h = \phi_{min} c_{min} + \phi_{org} c_{org} + \phi_{liq} c_{liq} + \phi_{ice} c_{ice} + \phi_{air} c_{air}$$

$$\phi_{min} = (1 - \theta_{sat})$$

$$\phi_{liq} = \theta$$

$$\phi_{min} + \phi_{org} + \phi_{liq} + \phi_{ice} + \phi_{air} = 1.0$$



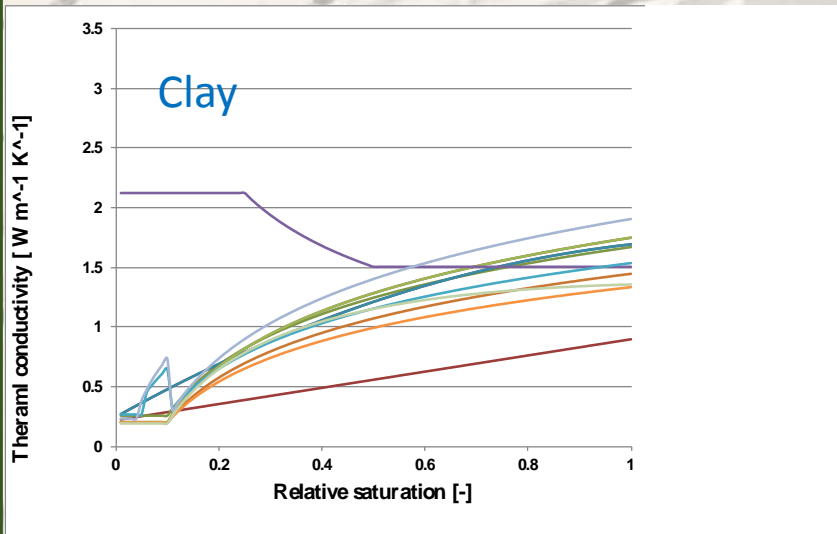
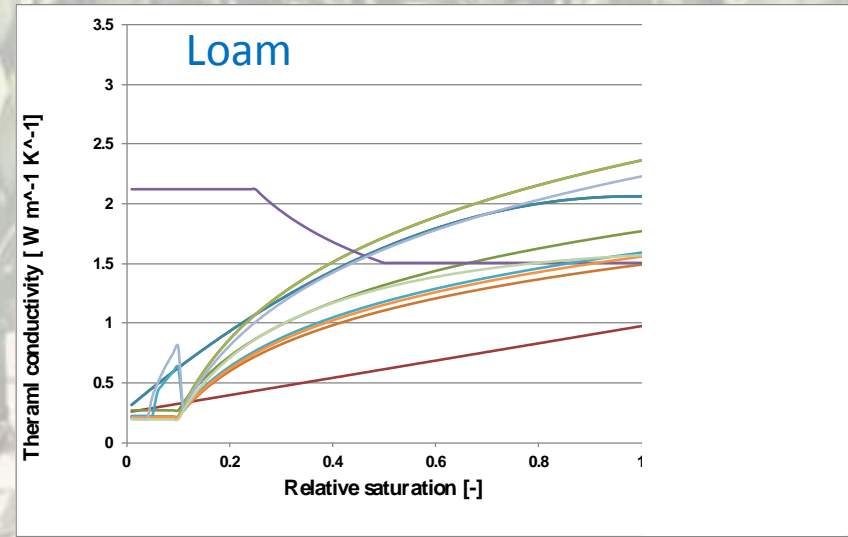
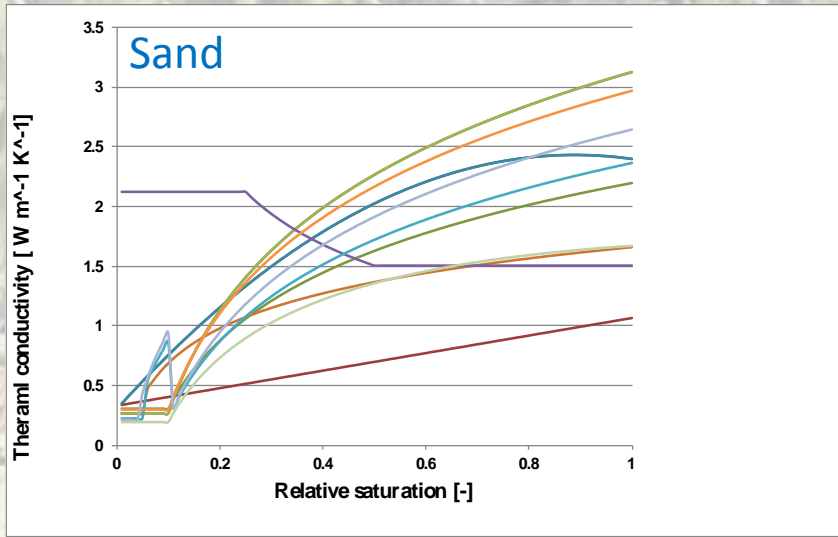
## CALCULATION OF MINERAL HEAT CAPACITY, $c_{min}$ OR $C_{min}$

- The main PTF for heat capacity relates to the way  $c_{min}$  or  $C_{min}$  is calculated. There are a number of options used in the LSMs:
    - (i) Employ the same value for all soil types
    - (ii) Use different values (tabulated) for each soil class,
    - (iii) Use different values per soil class, calculated as a function of texture:
- (i) One uses  $C_{min} = 1.942 \times 10^6$  (Johansen, 1975), as one of its options. Others use  $C_{min} = 2.0 \times 10^6$ ;  $c_{min} = 850 \text{ J kg}^{-1} \text{ K}^{-1}$ , or  $c_{min} = 733 \text{ J kg}^{-1} \text{ K}^{-1}$
- (ii) Two LSMs use the same values for  $C_{min} = \rho_{min} c_{min}$  for 11 USDA soil type as given in Pielke (2002) based on McCumber (1980), see also McCumber and Pielke (1981)
- (iii) A range of PTFs can be found, e.g. :

$$C_{min} = (f_{sand} C_{sand} + f_{clay} C_{clay}) / (f_{sand} + f_{clay})$$

$$C_{min} = f_{clay} C_{clay} + f_{sand} C_{sand} + f_{silt} C_{silt}$$

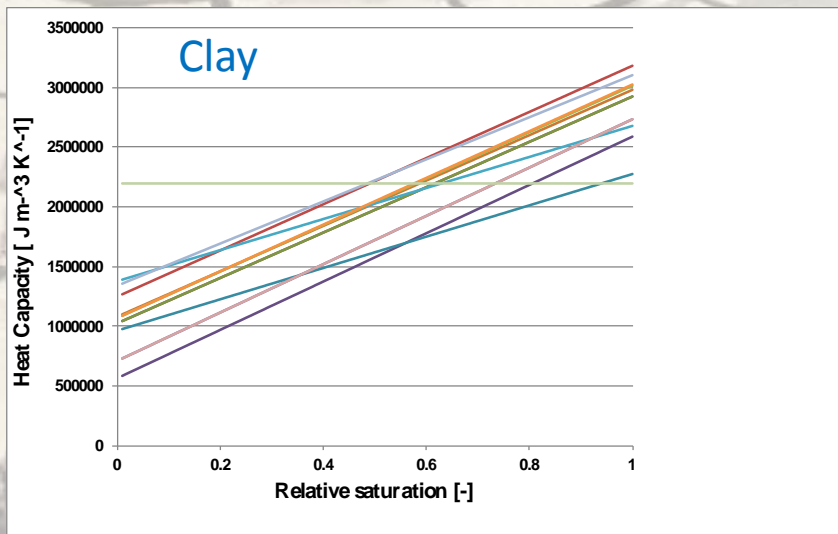
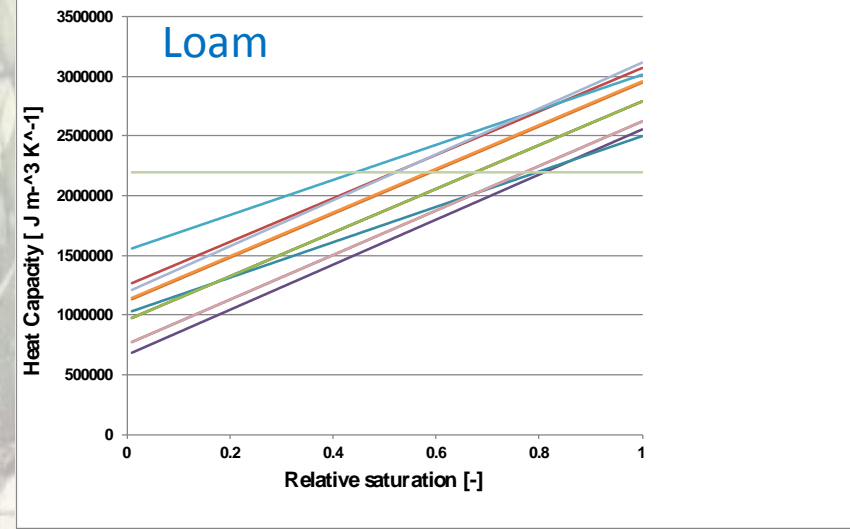
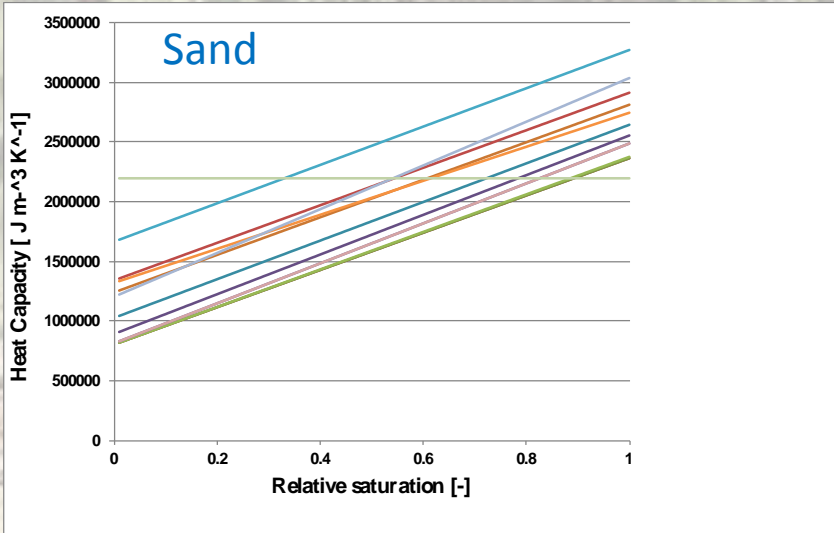
# RESULTS: THERMAL CONDUCTIVITY



## RESULTS, thermal conductivity

- Per soil type: large difference in  $\lambda$  between models
- Considerably different functional shapes between models

# RESULTS: HEAT CAPACITY



## RESULTS, HEAT CAPACITY

- Per soil type: considerable difference in  $C_h$  between models
- In some cases, different slopes between models

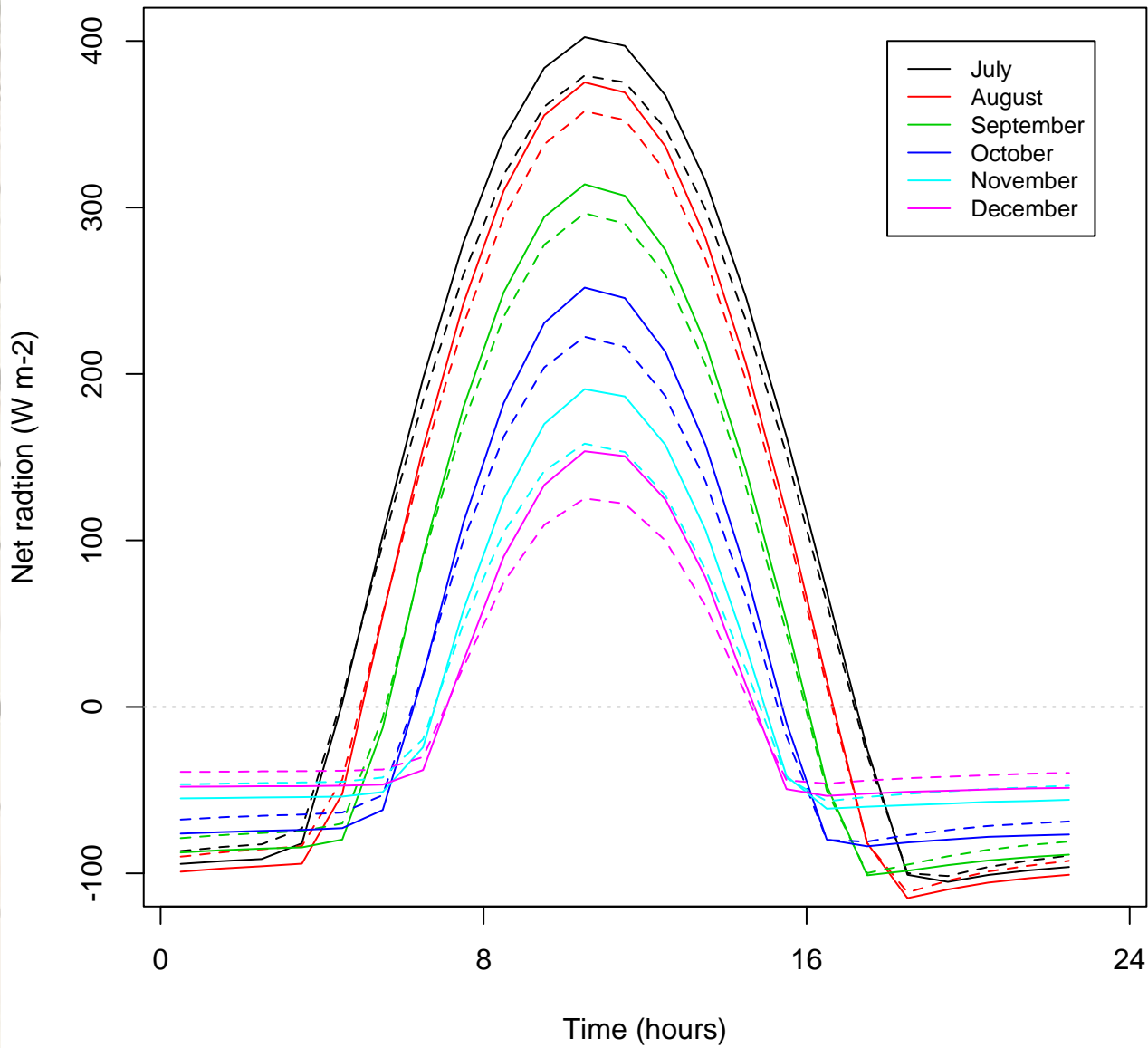


## MODEL RUNS, USING MODEL-SPECIFIC THERMAL (& hydraulic) properties

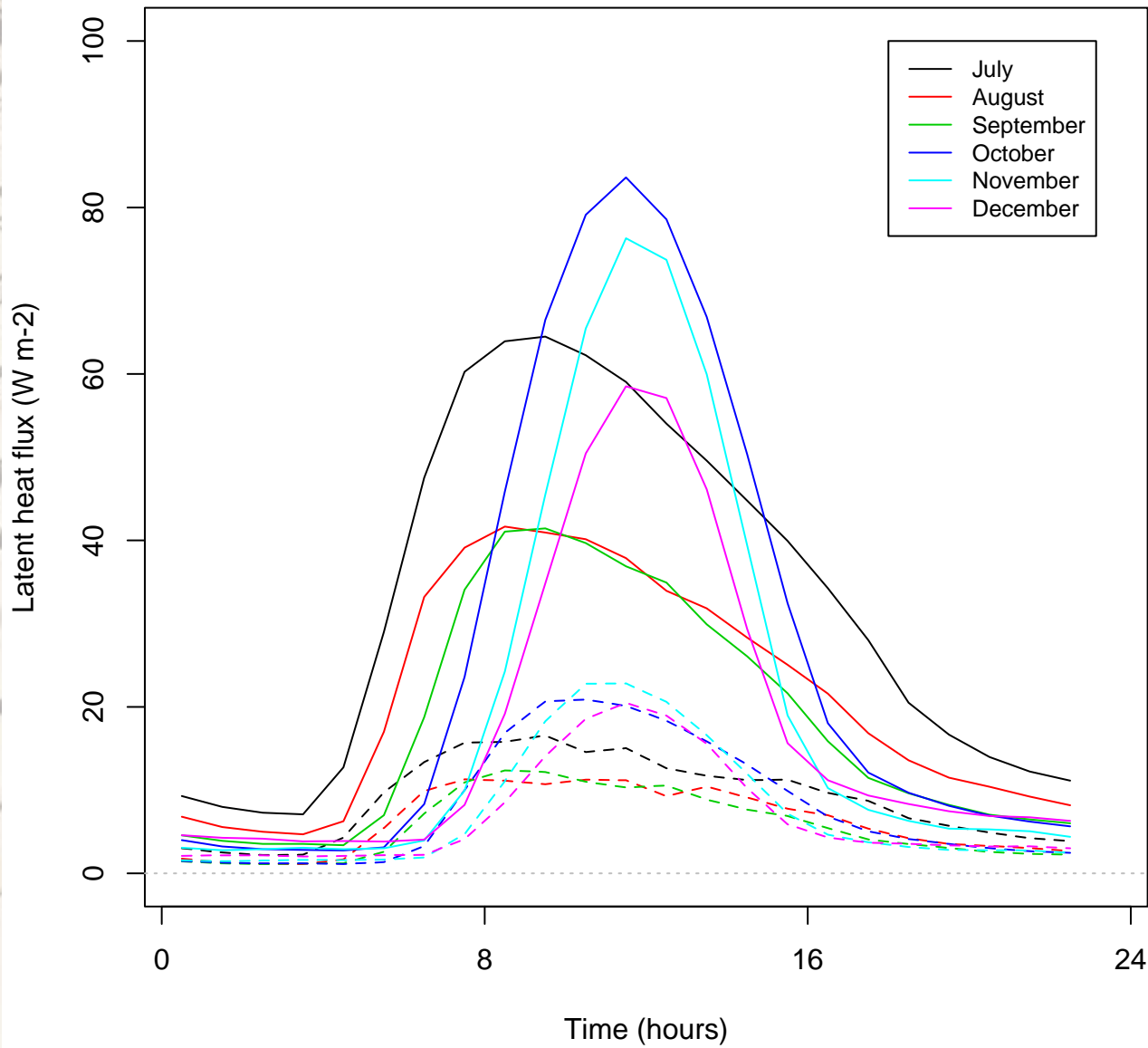
- Runs with Hydrus 1-D for 14 years (2001-2014) of half-hourly data from Avignon, model outputs are hourly
- 2 LSMs are compared in the next slides
- Bare soil, soil profile of 50 cm, no vapour flow, free drainage
- Sand, Loam, clay
- LSM thermal equations have been implemented into Hydrus-1D
- Effects on energy- and water balance have been investigated
- Effect on soil (surface) temperature and soil moisture content

COMPARISON USING HYDRUS MODEL

Net radiation, Sand, multi-year diurnal monthly average

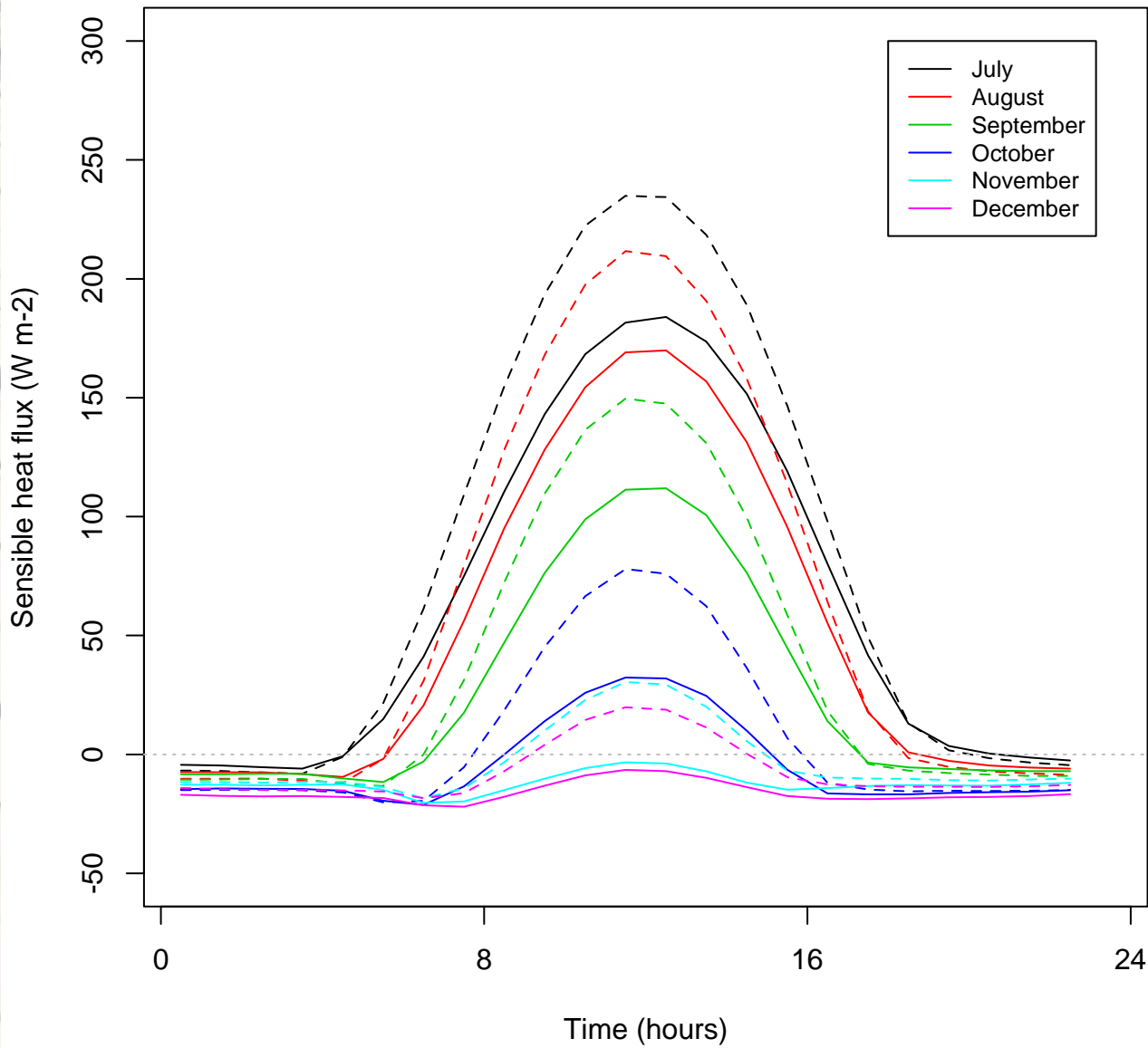


Evaporation, Sand, multi-year diurnal monthly average

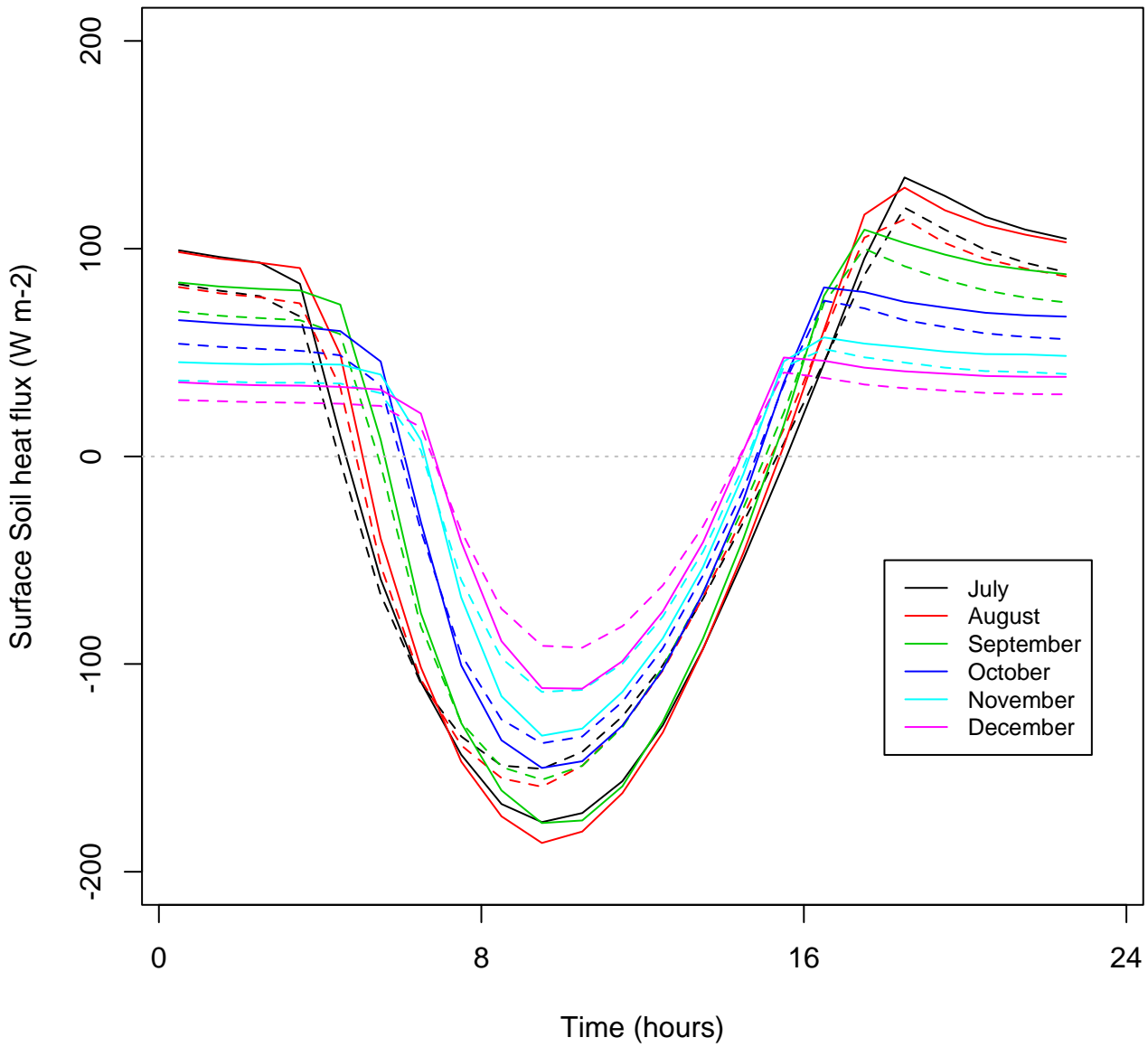




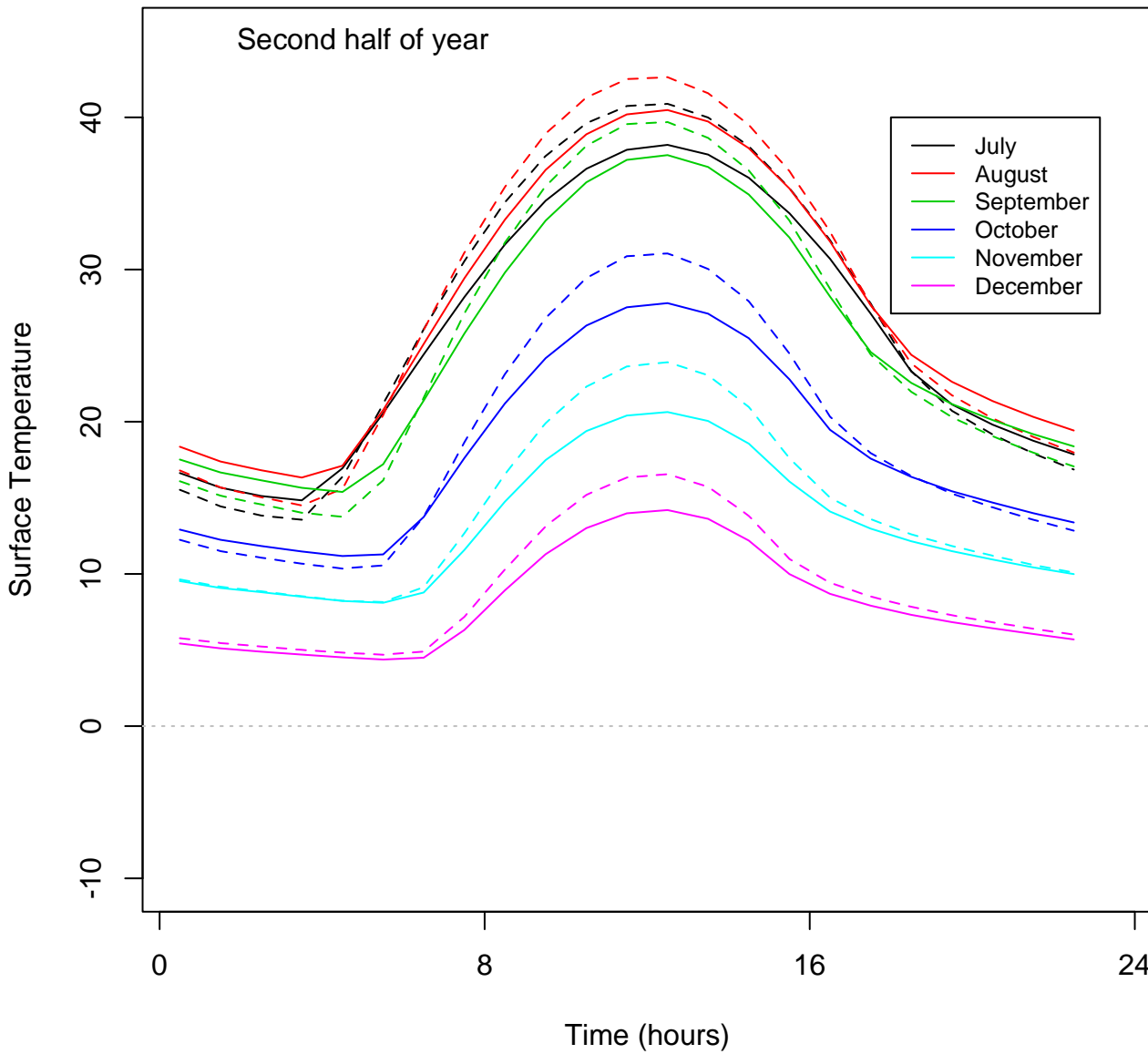
Sensible heat flux, sand, multi-year diurnal monthly average



Soil heat flux, sand, multi-year diurnal monthly average

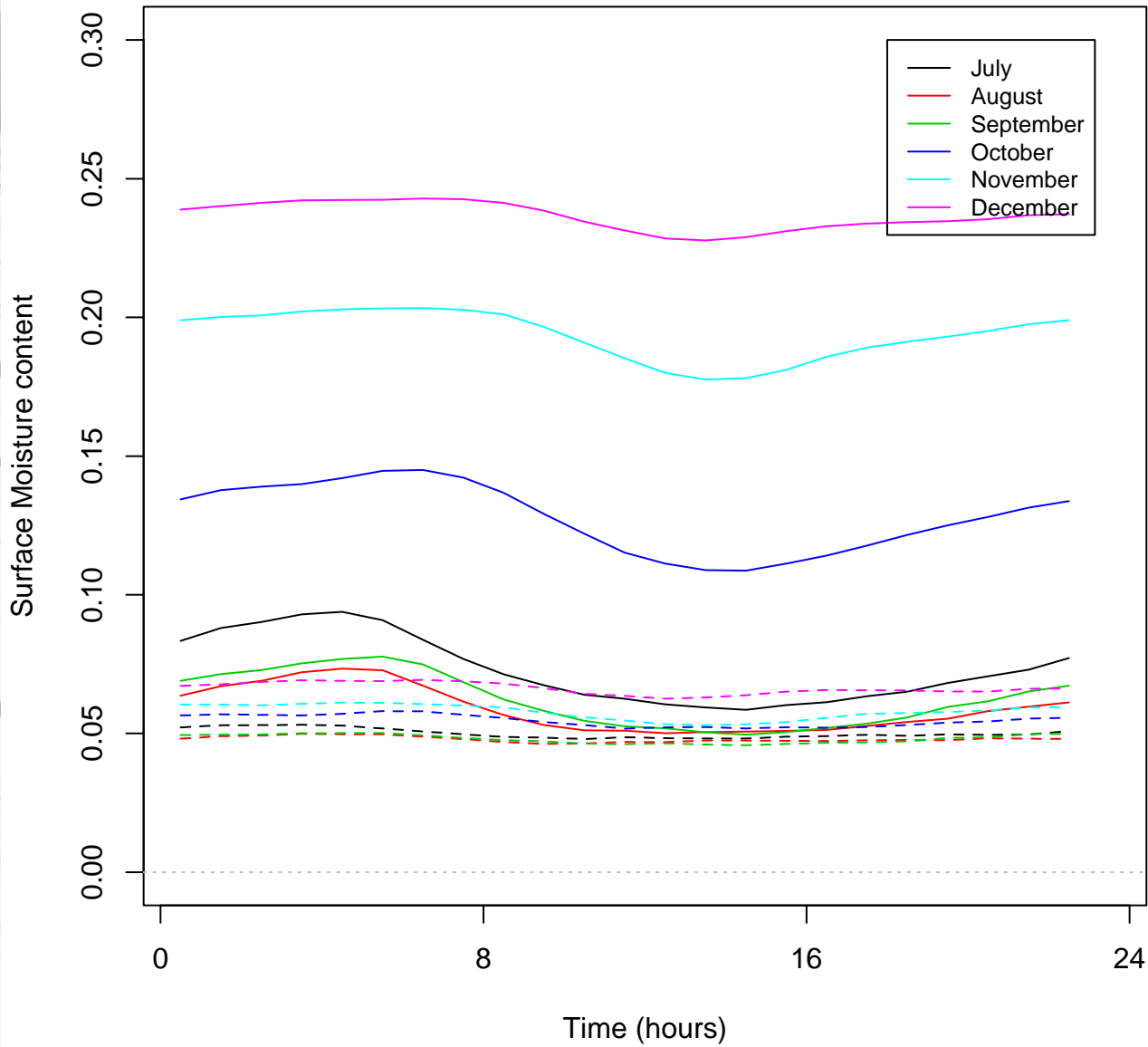


### Surface temperature, sand, multi-year diurnal monthly average



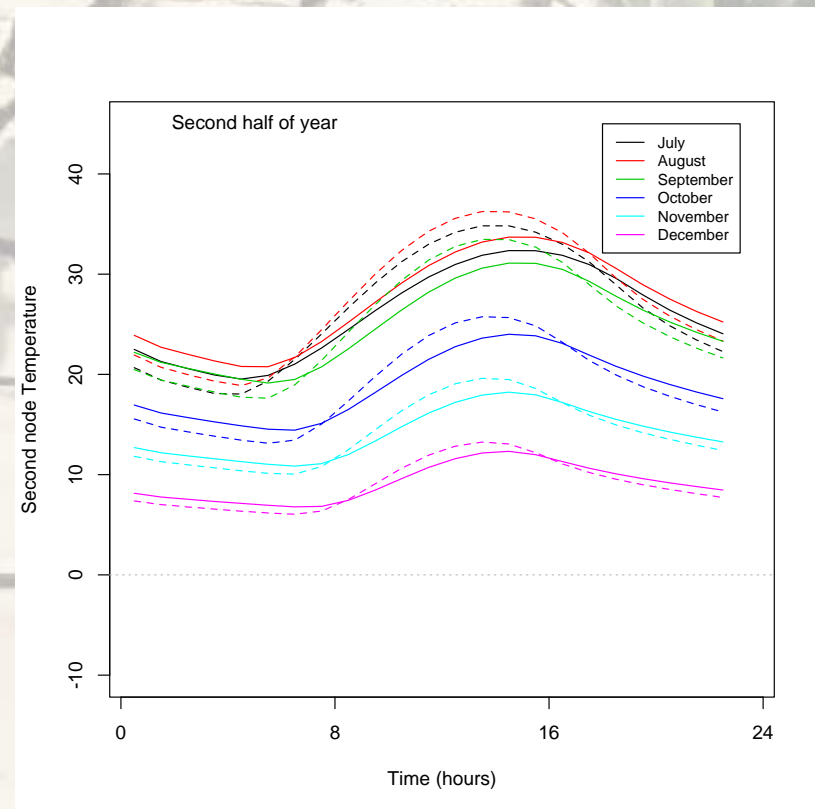
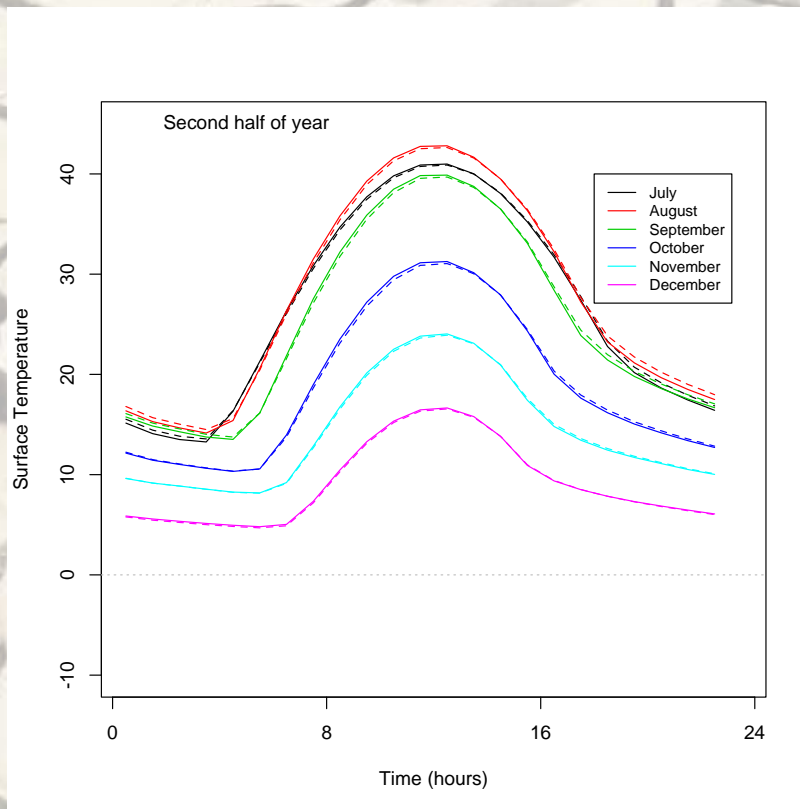


Surface SMC, sand, multi-year diurnal monthly average



Below: exact same hydraulic functions, but two different thermal functions, (solid line LSM 1, dashed line LSM 2)  
Small effect on EB fluxes and  $T_s$ , but considerable effect on deeper soil temperatures

Causes differences values, amplitudes and phase-shifts: implications for soil freezing and permafrost applications



## CONCLUSIONS

- Very different shapes for  $\lambda(\theta)$  curve, and considerable differences in  $C_h(\theta)$ , between LSM models
- Some LSM models have errors in their basic equations; some model teams have now corrected these
- PTFs for parameters in these thermal property functions vary considerably between models.
- They include a hydraulic PFT for porosity
- PFTs depend on soil texture and porosity/dry bulk density, as well as quartz content

## CONCLUSIONS, C'ED

- The combined effect of the choice of thermal and hydraulic equations on the energy and water balance is large
- When only the thermal properties differ, the main effect is on deeper soil temperatures
- This has implications for modelling of permafrost regions or soil respiration, for example



## NEXT STEPS

- Assess influence for vegetated surfaces (reduced)
- Use measured thermal properties to test validity of models
- Select preferred and/or adjust equations/PTFs
- Make recommendations to LS and Hydrological modellers